# Conduction in $Bi_2O_3$ -based oxide ion conductor under low oxygen pressure. II. Determination of the partial electronic conductivity

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In order to investigate the partial electronic conduction in the high oxide ion conductor of the system  $Bi_2O_3-Y_2O_3$  under low oxygen pressure, e.m.f. and polarization methods were employed. Although the electrolyte was decomposed when the  $P_{O_2}$  was lower than the equilibrium  $P_{O_2}$  of Bi,  $Bi_2O_3$  mixture at each temperature, the ionic transport number was found to be close to unity above that  $P_{O_2}$ . The hole conductivity  $(\sigma_p)$  and the electron conductivity  $(\sigma_n)$  could be expressed as follows,

$$\sigma_{\rm p} \Omega \,\rm{cm} = 5.0 \times 10^{2} (\dot{P}_{\rm O_{2}} \rm{atm}^{-1})^{1/4} \exp \left[-106 \,\rm{kJ} \, (RT \,\rm{mol})^{-1}\right]$$
  
$$\sigma_{\rm n} \Omega \,\rm{cm} = 3.4 \times 10^{5} (\dot{P}_{\rm O_{2}} \rm{atm}^{-1})^{-1/4} \exp \left[-213 \,\rm{kJ} \, (RT \,\rm{mol})^{-1}\right]$$

These values were much lower than the oxide ion conductivity under ordinary oxygen pressure.

# 1. Introduction

Takahashi and co-workers have reported the high oxide ion conduction in Bi<sub>2</sub>O<sub>3</sub>-based fcc solid solutions [1, 2]. As these materials are high conductivity conductors, various applications at lower temperatures are expected, e.g. in oxygen gauges, oxygen pumps and the like. For these purposes, the conduction behaviour under low oxygen pressures must be investigated, since, if an appreciable electronic conduction arises as a result of defect equilibrium at low  $P_{O_2}$ , the electrochemical measurements cannot be done correctly. In the previous paper, the current-blackening condition of the  $Bi_2O_3 - Y_2O_3$  electrolyte was reported [3]. We have now investigated the partial electronic conduction of the above oxide by e.m.f. measurements and the polarization method.

Electromotive force of a galvanic cell using a sample as the electrolyte is a most convenient method for determining the ionic transport number of solid electrolytes. Many cells have been constructed using various metal-metal oxide mixtures as the electrode materials and the domains of oxygen partial pressure where ionic conduction predominates were determined from the e.m.f. data [4-9]. However, in the case of the Bi<sub>2</sub>O<sub>3</sub>-based electrolyte, electrode materials which can be used as the  $P_{O_2}$  standard are limited to a few kinds of metal-metal oxide mixtures, since one component (Bi<sub>2</sub>O<sub>3</sub>) of the electrolyte is comparatively easily reduced under lower  $P_{O_2}$ , as reported in the previous paper [3] and since the mixtures having metals of low melting point are difficult to use at higher temperatures. Here, we have examined, whether the current-blackened oxide sample which exhibits an equilibrium  $P_{O_2}$  could be used as the electrode material of a galvanic cell.

The ionic transport number  $(t_{ion})$  can be determined generally by the above method. However, the contribution of hole and electron conduction in the solid electrolyte cannot be distinguished. Although Hebb-Wagner's polarization method can often be used for the purpose, this method requires that the ionic current is blocked [10–13]. This problem is still difficult to overcome in the case of oxide ion conductors. For this reason, Hartung employed an impervious Pt electrode covered by a high temperature glass on a hemispherical sample (yttria-stabilized zirconia) [14]. In this paper, we describe a method using a disc specimen having Ag electrodes, one of which was covered by soda glass.

### 2. Experimental

## 2.1. Galvanic cell method

A specimen having 27 mol%  $Y_2O_3$  was obtained by the same procedure as that reported previously [1, 3]. Two types of cells were constructed using this solid electrolyte,

M,  $MO_x(P_{O_2}, a)$ /electrolyte/Ag, air  $(P_{O_2}, c)$  (I)

and

blackened oxide  $(P_{O_2}, a)/electrolyte/$ 

Ag, argon 
$$(P_{O_s}, c)$$
 (II)

where  $P_{O_2}$ , a and  $P_{O_2}$ , c are the oxygen partial pressures in the anode and the cathode, respectively. For the cell (I),  $P_{O_2}$ , c was constant (0.21 atm) and  $P_{O_2}$ , a was changed using various





Fig. 1. Galvanic cells (schematic). (1) Glass packing; (2) sample; (3) anode material; (4) alumina crucible; (5) heater; (6) Ag lead; (7) CA thermocouple (8) CSZ tube; (9) Pt wire;  $(V_1)$  sample e.m.f.;  $(V_2)$  oxygen meter e.m.f.

mixtures of metal-metal oxide. For cell (II), the equilibrium oxygen partial pressure  $(P_{O_2}, eq)$  in the partially blackened oxide of the Bi<sub>2</sub>O<sub>3</sub>-Y<sub>2</sub>O<sub>3</sub> electrolyte was used as the low  $P_{O_2}$ , a standard [3] and  $P_{O_2}$ , c was variable. These cells are shown schematically in Fig. 1a and 1b. The electrolyte of the cell (I) is a disc specimen (13 mm diameter × 2 ~ 3 mm thickness) and is 93% dense. In the case of the cell (II), one end of Pt wire (0.5 mm diameter) was buried in a rod sample (5 mm diameter × 12 mm length) in order to obtain the blackened oxide as an electrode material directly.

The e.m.f. of the cell was measured at  $500 \sim 700^{\circ}$  C using a high impedance recorder. The  $P_{O_2}$  in argon gas used for the cell (II) was controlled by an oxygen pump employing a calcia-stabilized zirconia (CSZ) tube as an electrolyte. Argon gas introduced into the oxygen pump had been refined using spongy Ti, NaOH and P<sub>2</sub>O<sub>5</sub>. The  $P_{O_2}$  was checked by a CSZ oxygen meter.

#### 2.2. Polarization method

A specimen disc (13 mm diameter  $\times$  1 mm thickness) containing 27 mol% Y<sub>2</sub>O<sub>3</sub> was prepared by the ordinary method. The specimen was held in an electric furnace as indicated in Fig. 2. The Ag electrodes on both sample faces were 9 mm in diameter. The lower electrode was completely covered by commercial soda-glass in order to block the ionic current. The terminal voltage at a steady-state current was measured at 500 ~ 700° C under different values of  $P_{O_2}$ .



Fig. 2. Polarization cell (schematic). (1) Ag lead; (2) sample; (3) glass; (4) Pt lead; (5) alumina support (6) CA thermocouple; (7) heater.

#### 3. Results and discussion

#### 3.1. E.M.F. studies

According to Wagner's expression for oxide mixedconductors, the steady-state open circuit e.m.f. (E)may be written as

$$E = \frac{1}{4F} \int_{\mu_{O_2}, a}^{\mu_{O_2}, c} t_{\text{ion}} d\mu_{O_2}$$
$$= \frac{RT}{4F} \int_{\ln PO_2, a}^{\ln PO_2, c} t_{\text{ion}} d\ln P_{O_2} \qquad (1)$$

where F is Faraday's constant, R the gas constant, T the absolute temperature,  $t_{ion}$  the ionic transport number within the mixed conductor, and  $\mu_{O_2}$ and  $P_{O_2}$  the oxygen chemical potential and oxygen partial pressure, respectively. If the average ionic transport number is used, Equation 1 is rewritten as Equation 2.

$$E = t_{ion} \frac{RT}{4F} \ln \frac{P_{O_2}, c}{P_{O_2}, a}.$$
 (2)

For a predominantly ionic conductor  $(t_{ion} \approx 1)$ , the e.m.f. is given as follows,

$$E_{o} = \frac{RT}{4F} \ln \frac{P_{O_2}, c}{P_{O_2}, a}$$
(3)

Therefore, the ionic transport number for various electrolytes can be calculated from the ratio of E to  $E_0$ .



Fig. 3. Open circuit e.m.f. versus  $P_{O_2}$ , a relation for the cell (I) at 600° C.

Figure 3 indicates the e.m.f.'s of cell (I) at  $600^{\circ}$  C under various values of  $P_{O_2}$ , a. The  $P_{O_2}$ , a was changed from  $10^{-2}$  atm (air-argon mixture) to  $10^{-20}$  atm (Fe, FeO mixture). The measured values were almost equal to that calculated from Equation 3 (solid line) and were stable with time above  $10^{-13.1}$  atm, indicating that  $t_{ion}$  is nearly unity. But below  $10^{-13.1}$  atm, the e.m.f. values deviated from the calculated ones and were almost independent of  $P_{O_2}$ , a. The critical  $P_{O_2}$ , a of  $10^{-13.1}$  atm is the  $P_{O_2}$ , eq in the Bi, Bi<sub>2</sub>O<sub>3</sub> mixture. The electrolyte samples of such cells had been blackened on the anode sides and X-ray diffraction analysis showed partial decomposition into Bi metal. According to our previous paper [3], the blackened oxide containing Bi metal and Bi2O3-Y2O3

solid solution had a  $P_{O_2}$ , eq almost equal to that of a Bi, Bi<sub>2</sub>O<sub>3</sub> mixture. Therefore, it is apparent that the blackening was caused by the contact of the electrolyte with the metal-metal oxide mixtures having lower  $P_{O_2}$ , eq than  $10^{-13.1}$  atm at 600° C. This can be also supported by the fact that the e.m.f. values of such cells correspond almost to the value at  $P_{O_2}$ ,  $a = 10^{-13.1}$  atm at 600° C. In order to obtain the low  $P_{O_2}$  standard directly

In order to obtain the low  $P_{O_2}$  standard directly in the blackened oxide, the oxide sample around the Pt wire in the case of the cell (II) was electrolysed partially into Bi metal under unpurified argon gas ( $P_{O_2} \approx 10^{-4}$  atm). Fig. 4 represents the temperature dependence of the e.m.f. of cell (II) at  $P_{O_2}$ ,  $c = 10^{-4}$  atm. The e.m.f. at each temperature coincides with the value calculated from Equation 3 using the  $P_{O_2}$  in the blackened oxide (solid line)



Fig. 4. Open circuit e.m.f. versus temperature relation for the cell (II) at  $P_{O_2}$ , c = 10<sup>-4</sup> atm.



Fig. 5. Open circuit e.m.f. versus  $P_{0_2}$ , c relation for the cell (II) at 600° C ( $\triangle$ ) the e.m.f. of the cell (IV).

[3]. Therefore, these results show that: (i) this type of sample can retain the low  $P_{O_2}$  in the blackened oxide, which can be used as the  $P_{O_2}$  standard of a galvanic cell; (ii)  $t_{ion}$  of this sample is close to unity at  $P_{O_2}$ ,  $c \ge 10^{-4}$  atm between 500 and 700° C even when  $P_{O_2}$ , a is very low ( $\approx 10^{-13}$  atm).

When the  $P_{O_2}$ , c of cell (II) was lowered, the e.m.f. variation in Fig. 5 was observed at 600° C. If the  $t_{ion}$  of the electrolyte is unity and the electrode reaction of oxygen is reversible over a wide range of  $P_{O_2}$ , c, the e.m.f. relation shown by the solid line should be observed. The measured e.m.f. is obviously much lower than this below a certain  $P_{O_2}$ . This denotes the presence of mixed ionic and electronic conduction in the sample. However, if the partial electronic conduction causes electrode polarization, the ratio of ionic and electronic conduction cannot be determined in this case. The following cells were constructed to measure the ionic transport number at lower oxygen pressure,

Bi, 
$$Bi_2O_3$$
/sample electrolyte/Cu, Cu<sub>2</sub>O (III)

Table. 1. Electronic conductivity  $(\sigma_e)$  and ionic transport number  $(t_{ion})$  calculated using the cells [III] and [IV].

° C	Cell III		Cell IV	
	$\sigma_{\rm e}(\Omega^{-1} {\rm ~cm^{-1}})$	tion	$\sigma_{\rm e}(\Omega^{-1}{\rm cm}^{-1})$	t <sub>ion</sub>
500	$4.16 \times 10^{-5}$	0.995		0.999
600	$1.64 \times 10^{-4}$	0.997	$3.57 \times 10^{-6}$	0.999
700	$9.20  imes 10^{-4}$	0.995	1.90 × 10 <sup>-5</sup>	0.999

## Bi, Bi<sub>2</sub>O<sub>3</sub>/sample electrolyte/CuO, Cu<sub>2</sub>O. (IV)

These galvanic cells showed much lower e.m.f.'s than the  $E_{o}$  values calculated from the  $\Delta G_{f}$  values of the anode and cathode materials (Fig. 5). However, if each  $E_0$  is applied to the cell from an outer source in changing the polarity, no ionic current passes through the sample and the observed current is electronic. In this condition, the electronic conductivity  $(\sigma_e)$  of the sample is obtained from the electronic current and the terminal voltage [15]. In Table 1, this result and  $t_{ion}$  calculated using the above parameters are presented. As a result, the sample electrolyte used here was found to be a predominantly ionic conductor over a wide range of  $P_{O_2}$  (e.g.  $\ge 10^{-13.1}$  atm at 600° C). At lower values of  $P_{O_2}$  than that, the oxide sample was reduced and decomposed partially into Bi metal. Thus, the small e.m.f. in the low  $P_{O_2}$ , c range in Fig. 5 can be explained by the polarization of the electrode reaction caused by partial electronic conduction.

# 3.2. Hole and electron conduction

The steady-state polarization current density in an anionic conductor has been shown by Patterson *et al.* [13] to obey the following relation:

$$J_{ss} = K\sigma_n(\exp U - 1) + K\sigma_p(1 - \exp - U) \quad (4)$$

in which K = RT/LF and U = EF/RT, and E is the e.m.f. applied to the cell, L the thickness of electrolyte, and  $\sigma_n$  and  $\sigma_p$  the electron and hole conductivities for the electrolyte, equilibrated with oxygen at the appropriate pressure. Equation 4 can be changed into Equation 5:

$$J_{ss}/K(1 - \exp - U) = \sigma_n \exp U + \sigma_p.$$
 (5)

Therefore,  $\sigma_n$  and  $\sigma_p$  can be obtained from the slope and intercept of the  $J_{ss}/K(1 - \exp - U)$  versus exp U relation.

In order to perform polarization measurements, a blocking electrode must be established. Here, the ionic current was blocked by covering the Ag electrode on a disc specimen with a commercial sodaglass softened at 800° C. No chemical reaction between the electrolyte and the glass was observed below 700° C. Fig. 6 represents the data at 500 ~ 700° C in air. The same measurements were done in oxygen and argon gas and in the  $P_{O_2}$ , eq of the CuO, Cu<sub>2</sub>O mixture. However, as the CuO, Cu<sub>2</sub>O



Fig. 6. Data for the polarization studies in air.

did not behave as a reversible electrode as mentioned above, no satisfactory measurements could be made in this case. Values of  $\sigma_n$  and  $\sigma_p$  calculated from the slopes and the intercepts are presented in Fig. 7, with the oxide ion conductivity of this material, as a function of the reciprocal of the absolute temperature [1]. The activation energies under different  $P_{O_2}$  values for hole or electron conduction are almost comparable and they are calculated to be 106 kJ mol<sup>-1</sup> and 213 kJ mol<sup>-1</sup>, respectively. The  $\sigma_{\rm p}$  and  $\sigma_{\rm n}$  versus  $P_{\rm O_2}$  data are indicated in Fig. 8. The slopes show the relations of  $\sigma_{\mathbf{p}} \propto P_{\mathbf{O}_2}^{1/4}$  and  $\sigma_{\mathbf{n}} \propto P_{\mathbf{O}_2}^{-1/4}$ , indicating that the following defect equilibria are established in the presence of a large number of oxide ion vacancies due to the fluorite-type structure of the sesquioxide.



Fig. 7. Hole and electron conductivity of the  $Bi_2O_3-Y_2O_3$  electrolyte in air and argon.



Fig. 8.  $P_{\Omega_2}$  dependence of the hole and electron conductivities of the Bi<sub>2</sub>O<sub>3</sub>-Y<sub>2</sub>O<sub>3</sub> electrolyte; ( $\triangle$ ) the electronic conductivity obtained using the cell (III).

$$\frac{1}{2}O_2 + V_0^{"} \longrightarrow O_0 + 2h^+$$
(6)

$$O_o \longrightarrow V_o'' + 2e^- + \frac{1}{2}O_o.$$
 (7)

The electronic conductivity ( $\sigma_{e}$ ), calculated from the e.m.f.  $(E_{0})$  for the cell [III], (see Equation 3), is considered to correspond to the electron conductivity  $(\sigma_n)$ , since the  $P_{O_2}$ , a and  $P_{O_2}$ , c values of the cell [III] are low and close to one another. The  $\sigma_{\rm e}$  values are also plotted against the  $P_{\rm O_2}$ , eq values of the Cu, Cu<sub>2</sub>O mixtures at each temperature in Fig. 8, and lie almost on the extrapolated lines. These results also indicate partial non-stoichiometry as expressed in Equations 6 and 7. However, the contribution of electronic conduction to the total conductivity was found to be rather lower in the higher  $P_{O_2}$  range than in the  $P_{O_2}$ , eq of the Bi, Bi<sub>2</sub>O<sub>3</sub> mixture. The hole and electron conductivity of the  $Bi_2O_3$ - $Y_2O_3$  electrolyte can be expressed using the results of the temperature and  $P_{O_2}$  dependence of both conductivities as follows;

$$\sigma_{p}\Omega \text{ cm} =$$
5.0 × 10<sup>2</sup> (P<sub>O<sub>2</sub></sub> atm<sup>-1</sup>)<sup>1/4</sup> exp [- 106 kJ(RT mol)<sup>-1</sup>]  

$$\sigma_{n}\Omega \text{ cm} =$$
(8)  
3.4 × 10<sup>5</sup> (P<sub>O<sub>2</sub></sub> atm<sup>-1</sup>)<sup>-1/4</sup> exp [- 213 kJ(RT mol)<sup>-1</sup>]  
(9)

# 4. Conclusion

As a result of this investigation, it can be stated that the electrolyte domain (where  $t_{ion} \ge 0.99$ ) for the Bi<sub>2</sub>O<sub>3</sub>-Y<sub>2</sub>O<sub>3</sub> oxygen ion conductor extends down to the  $P_{O_2}$  given by the decomposition of the oxide electrolyte (10<sup>-13.1</sup> atm at 600° C). That is, the oxide ion conductivity of the electrolyte is, at least, two orders of magnitude higher than the partial electronic conductivity between 500 and 700° C under a non-reducible  $P_{O_2}$  atmosphere. The hole and electron conductivity can be expressed by the following equations:

$$\sigma_{p}\Omega \text{ cm} = 5.0 \times 10^{2} (P_{O_{2}} \text{ atm}^{-1})^{1/4}$$

$$\times \exp \left[-106 \text{ kJ} (RT \text{ mol})^{-1}\right]$$

$$\sigma_{n}\Omega \text{ cm} = 3.4 \times 10^{5} (P_{O_{2}} \text{ atm}^{-1})^{-1/4}$$

$$\times \exp \left[-213 \text{ kJ} (RT \text{ mol})^{-1}\right].$$

This oxide ion conductor can be used as the electrolyte of an oxygen gauge to measure comparatively high  $P_{O_2}$  at lower temperatures using a high  $P_{O_2}$ , c standard e.g. oxygen or air.

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